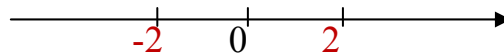


2.7 Absolute Value Equations and Inequalities

Remember: Absolute value represents “**distance from zero**”, so $|x| = 2$ tells us that x is 2 steps from zero; therefore $x = 2$ or $x = -2$.



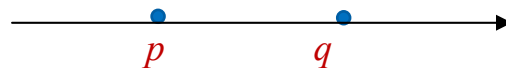
Generally, to solve an absolute value equation we must consider **two cases**

$$|\text{expression}| = k,$$

$$\text{expression} = k \text{ or } \text{expression} = -k$$

and solve them separately.

The solution set usually consists of two numbers $\{p, q\}$.



Example 1: Solve.

a) $|3x + 2| = 14$

b) $2|x| - 1 = 3$ *isolate abs. value first!*

c) $\left| \frac{3x+2}{3} \right| = 5$

d) $|1 - x| = -2$ *abs. value can't be negative!*

To solve equations with two absolute values, follow the pattern: $|\text{expr. A}| = |\text{expr. B}|$

$$\text{expr. A} = \text{expr. B} \text{ or } \text{expr. A} = -\text{expr. B}$$

Example 2: Solve.

a) $\left| \frac{x}{2} - 5 \right| = \left| 3 - \frac{x}{2} \right|$

Generally, there are two types of absolute value inequalities:

$ expression < k$ \Downarrow $-k < expression < k$	$ expression > k$ $\swarrow \quad \searrow$ $expression < -k \text{ or } expression > k$
	

Example 3: Solve. Graph the solution on a number line and state it in interval notation.

a) $|-1 - 2x| < 5$

b) $\left|\frac{x-2}{3}\right| \geq 4$

c) $-|2x - 3| \geq -7$

d) $\left|\frac{1}{3}x + 7\right| + 5 > 6$

Watch these special cases:

e) $|5x + 2| < -8$

f) $-2|3x - 4| < 16$